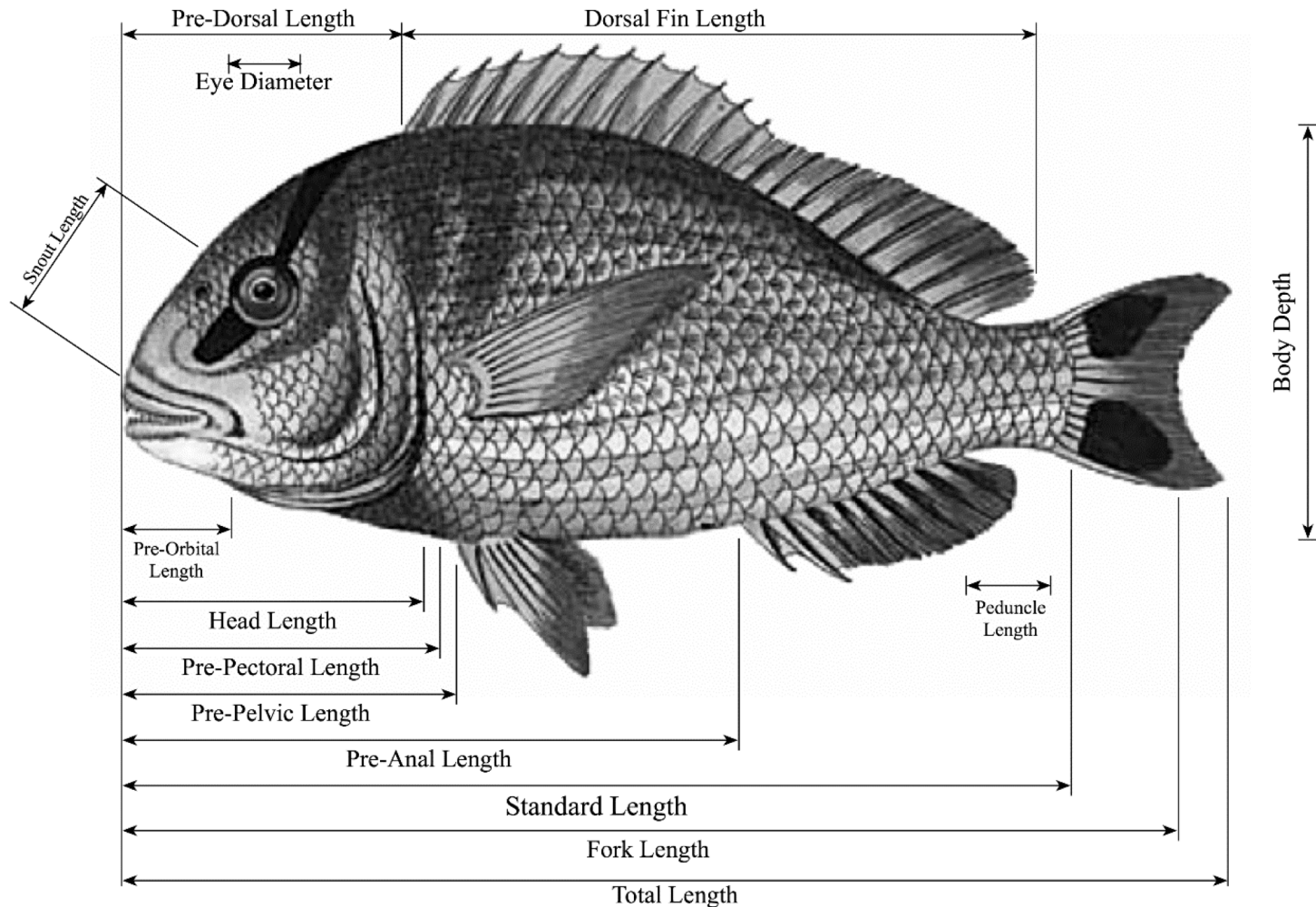


# Métodos comparativos para dados multivariados

# Outline da aula

- Breve histórico da morfometria geométrica
- “revolução” na morfometria na década de 1980
- Principais conceitos e aplicações
- Principais métodos comparativos para dados multivariados
  - Taxa evolutiva
  - Ajuste de modelos evolutivos levando em conta correlação entre traits
  - Mudança de estado ótimo ao longo da filogenia

# Lógica da morfometria tradicional



# Problemas com a morfometria tradicional

- Usa várias medidas lineares, razões e ângulos mas que não capturam a *posição* dos marcos anatômicos
- Difícil estabelecer homologia entre estruturas
- Medidas lineares não capturam geometria
- Geram várias variáveis correlacionadas que precisam passar por redução (e.g., PCA) antes de serem usadas
- Confunde **tamanho** e **formato**
- Sempre o PC 1 é relacionado com tamanho

# Vantagens da GM

- Consegue separar Tamanho de Formato, além de fornecer técnicas de visualização
- Permite medir formas não só em 2D como em 3D

# Definição de forma

*“all the geometric information that remains when location, scale and rotational effects are filtered out from an object”*

Kendall 1977



David Kendall

Desenvolveu o aparato matemático/geométrico para medir forma



Fred Bookstein

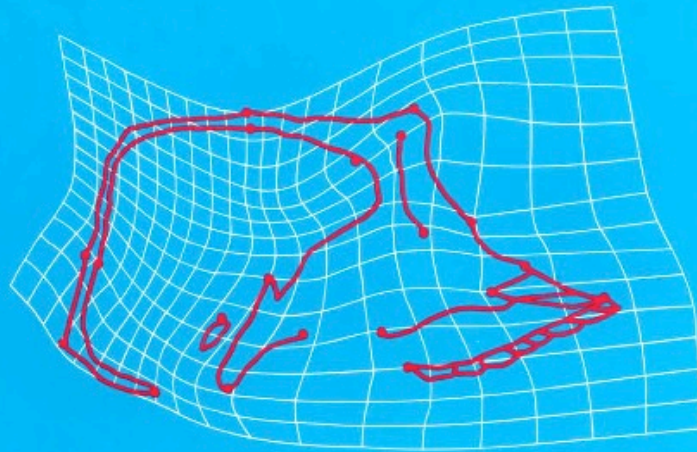
Desenvolveu métodos estatísticos que hoje em dia fazem parte do “catecismo” da GM



James Rholff

Adaptou Procrustes para dados de landmark

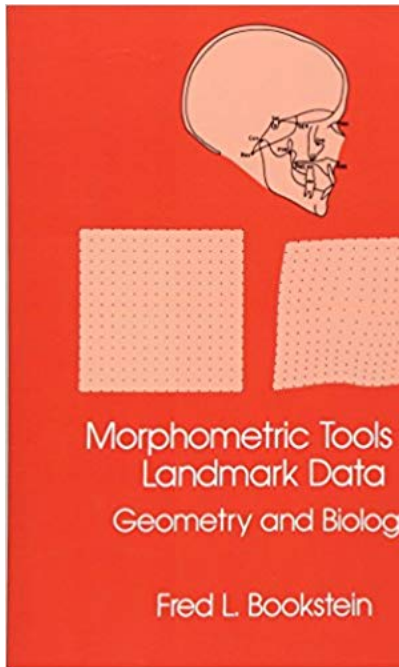
**Proceedings of the  
Michigan Morphometrics Workshop**



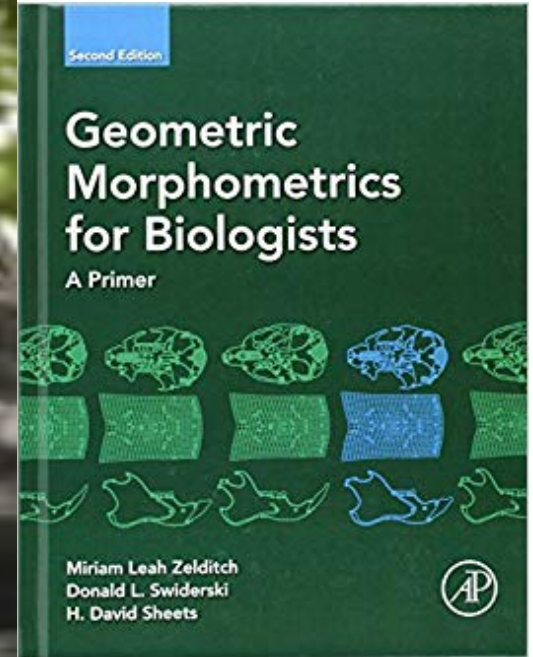
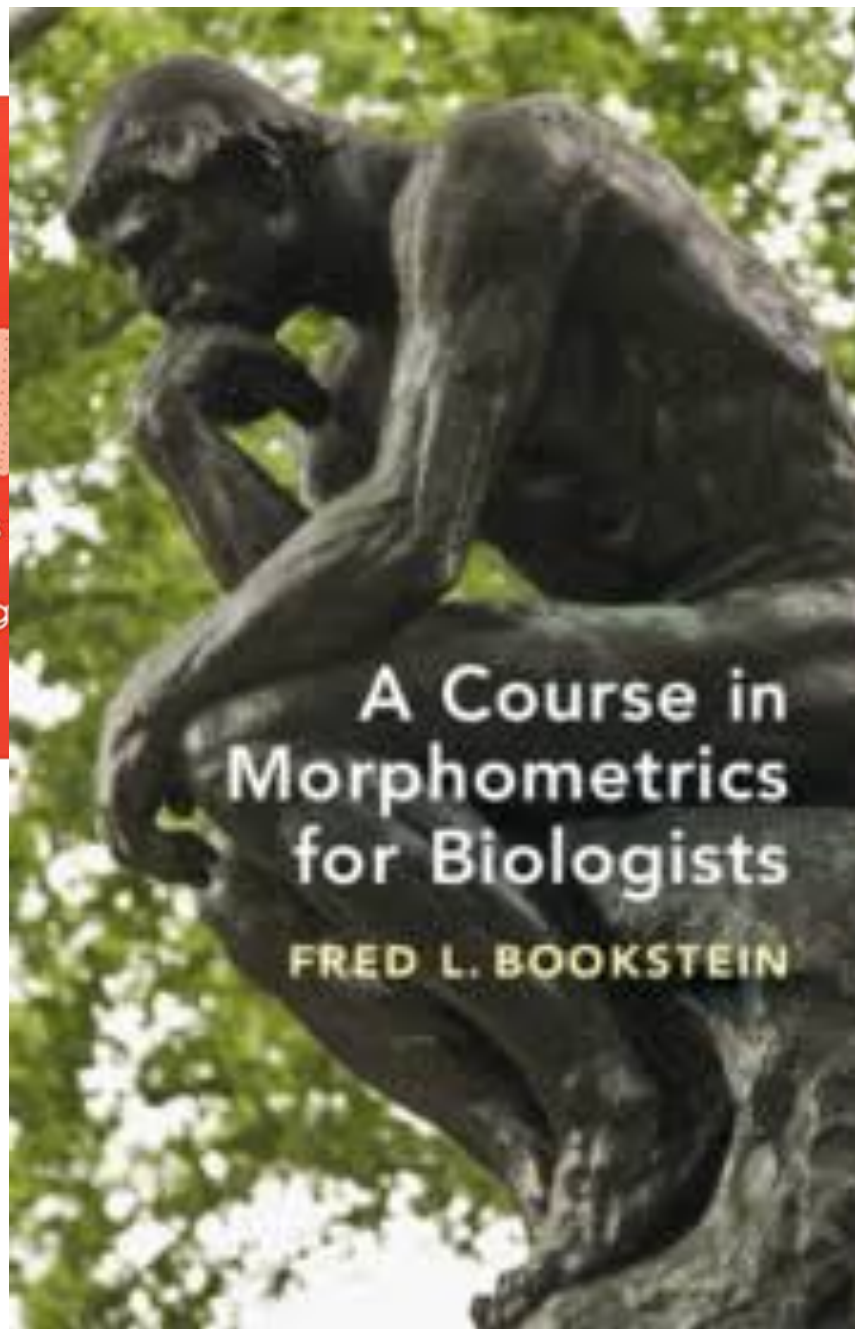
Edited by  
**F. James Rohlf**  
**Fred L. Bookstein**

Special Publication Number 2  
The University of Michigan Museum of Zoology

1990

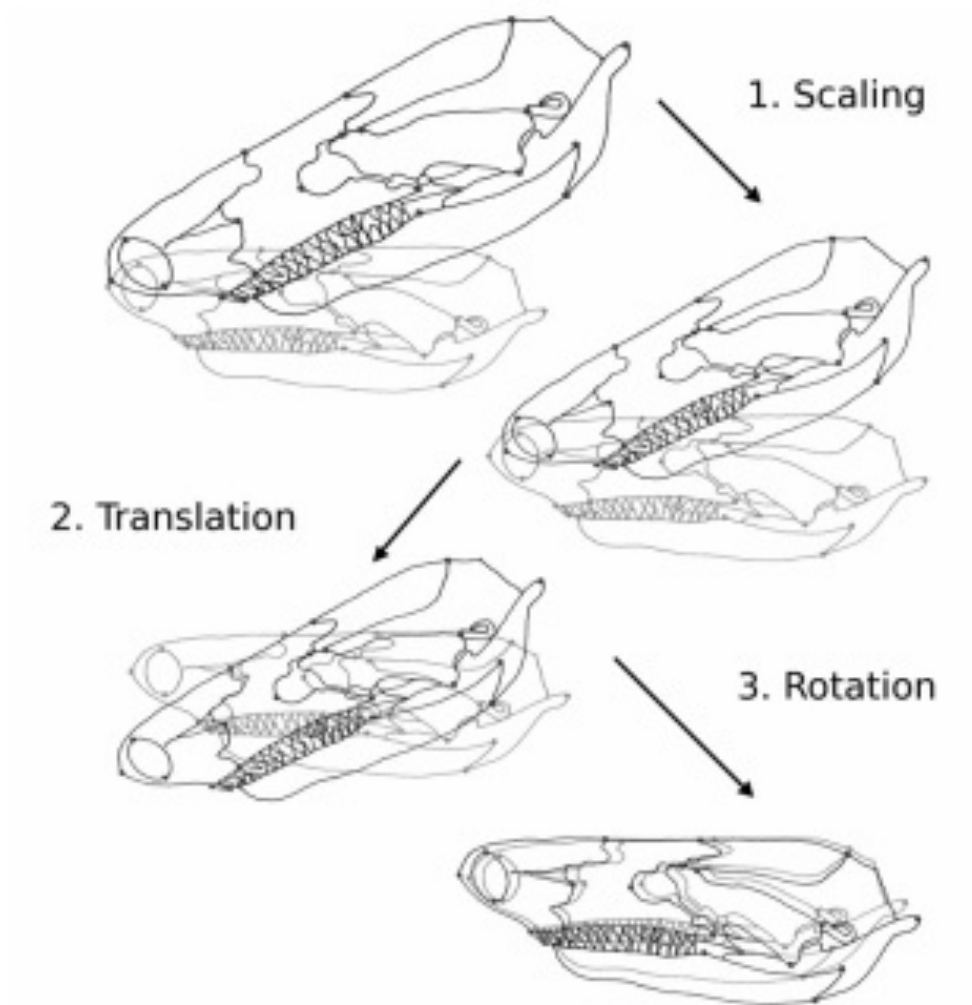


1992

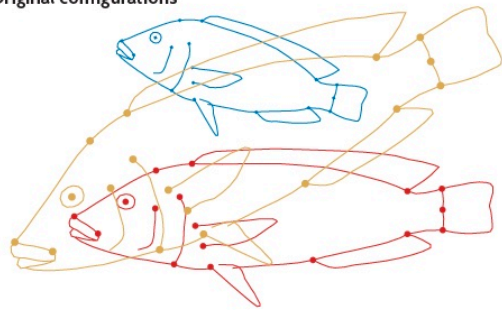


2004 e  
2012

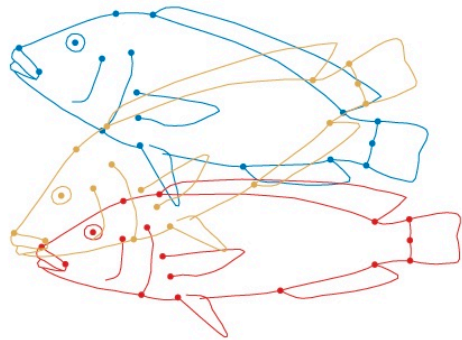
# Operações que não mudam o formato do objeto



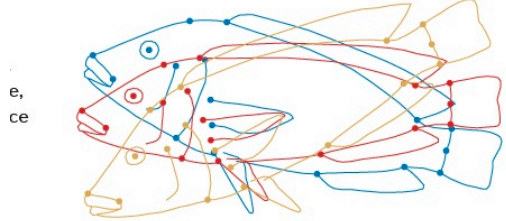
Original configurations



Scaling to the same size



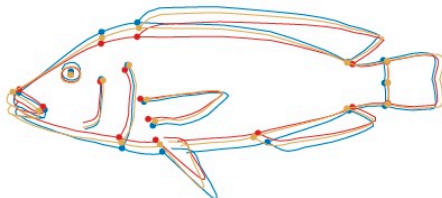
Translation to the same location



between

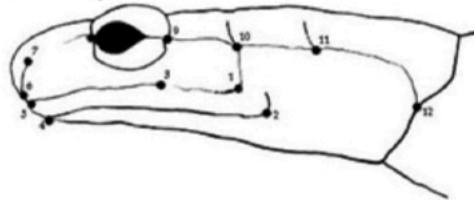


Rotation to optimal fit

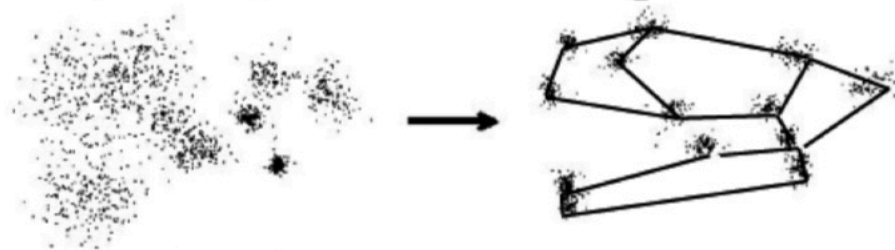


between

1) Digitize landmarks

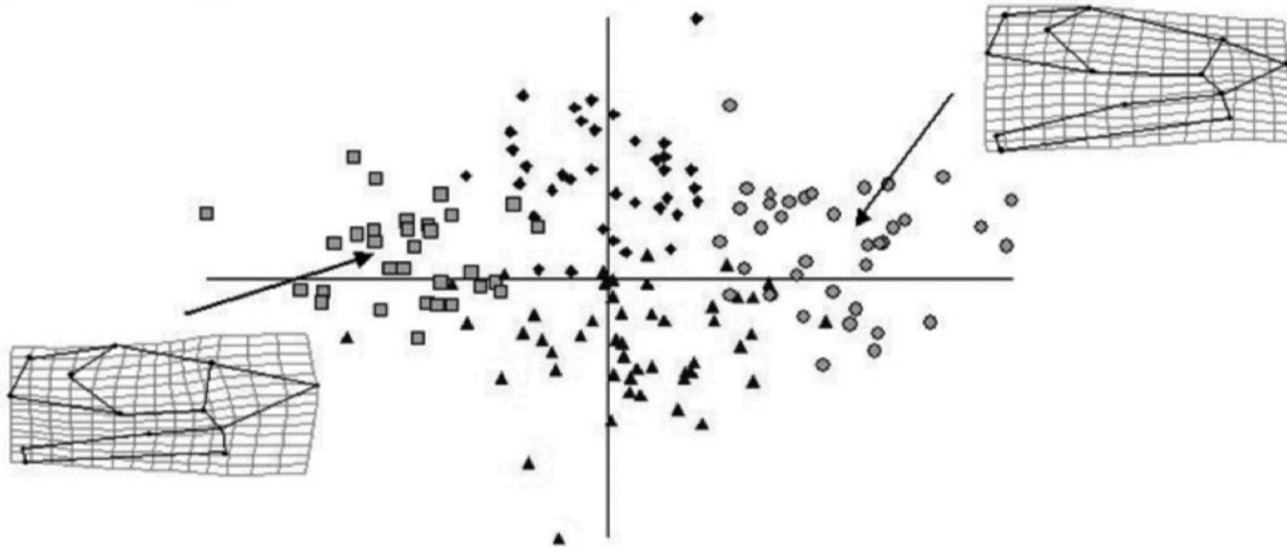


2) GPA (remove non-shape variation)



3) Statistical analysis (e.g., MANOVA)

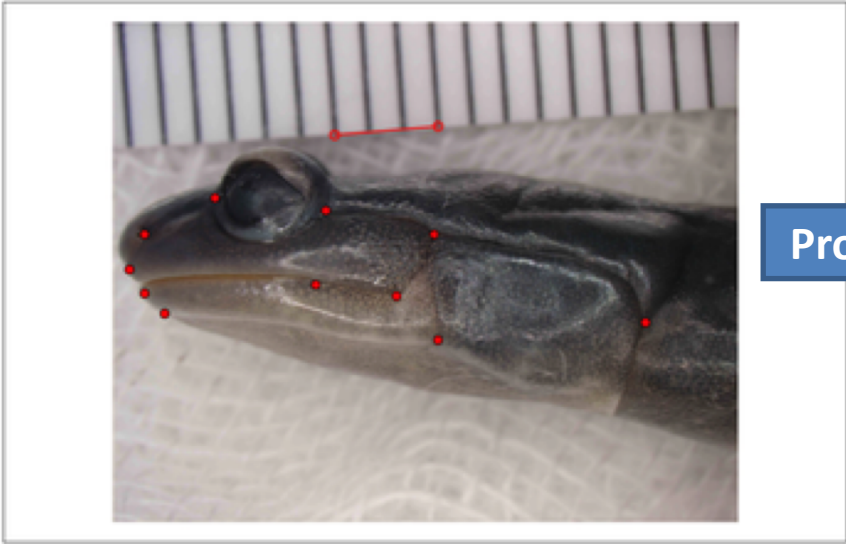
4) graphical depiction of results (statistical and morphometric)



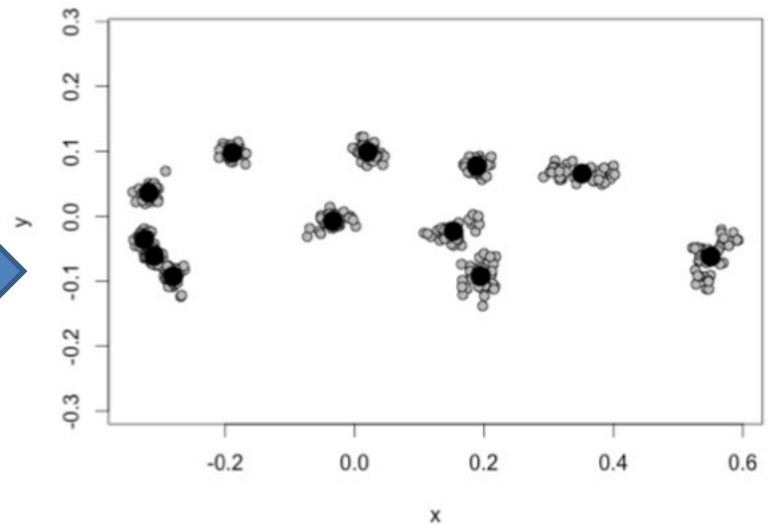
- Landmarks: coordenadas cartesianas (X,Y) que são homólogas entre exemplares (ou espécies)
- Semi-landmarks: não homólogos, usados para descrever contornos
  - Antigamente eram usados outline techniques

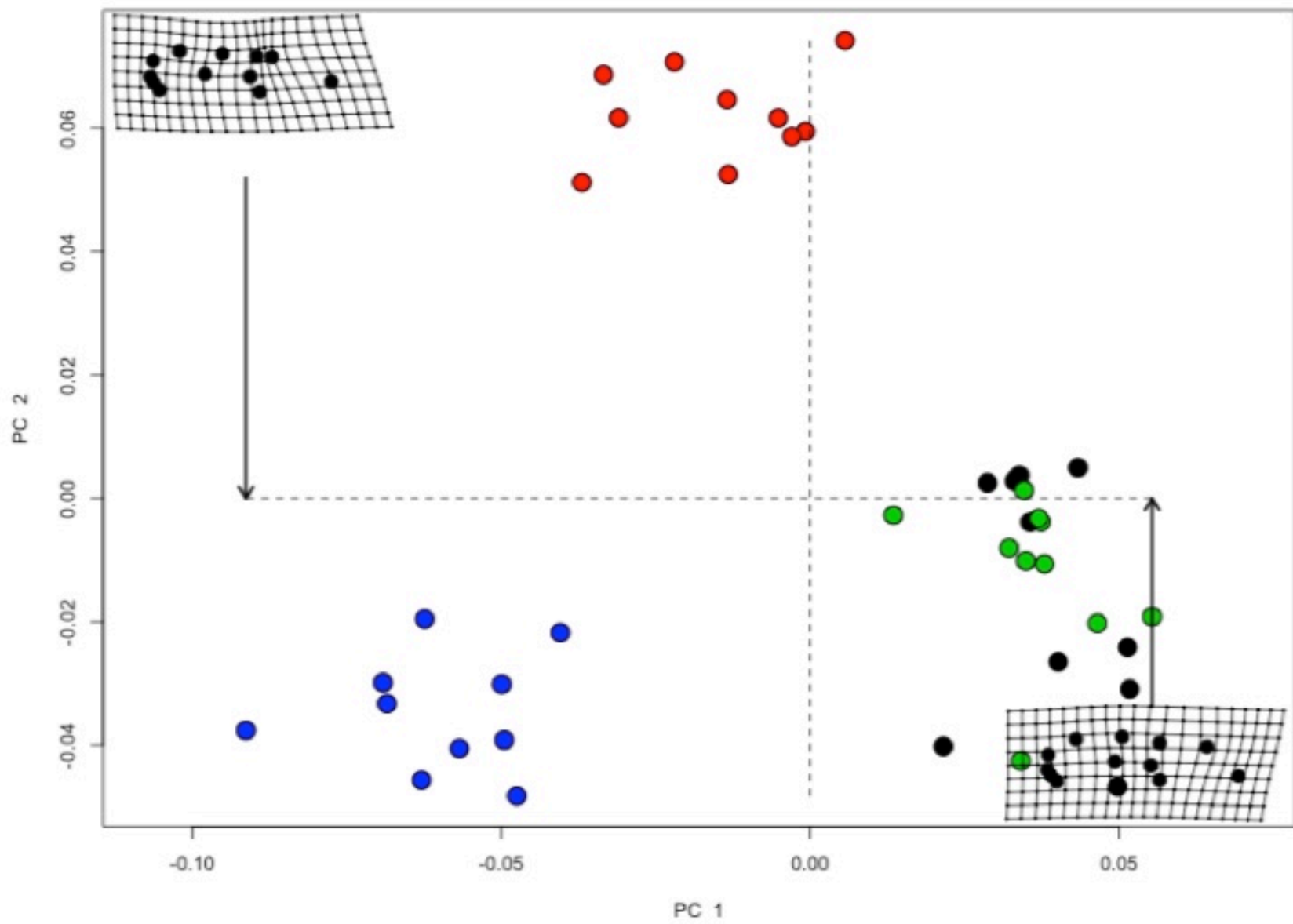
Locator active (Esc to finish)

Finish

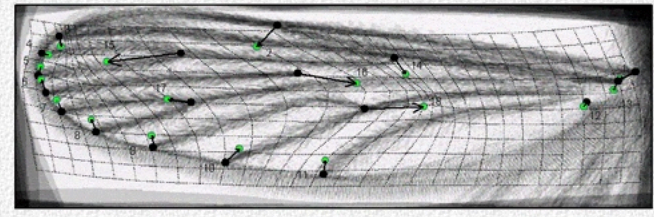
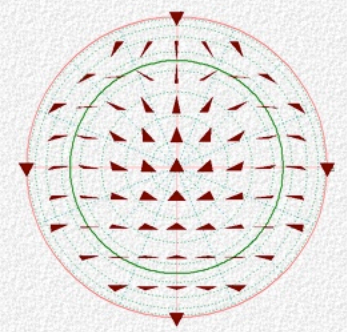


Procrustes





# Morphometrics at SUNY Stony Brook



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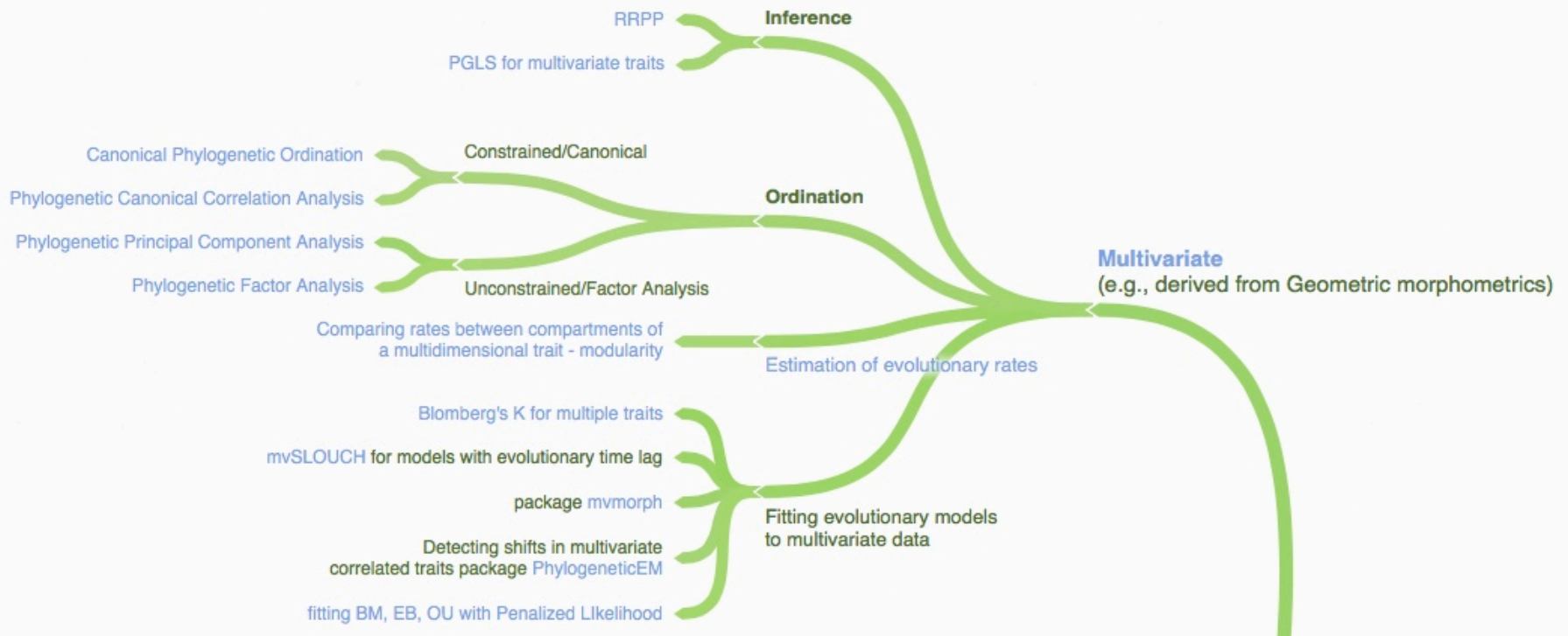
According to our counter, this site has now been accessed by people in more than 8050 cities around the world. The field is expanding! See the new map below for visits since April 2016.



# Métodos comparativos

# O que vimos até aqui?

- Formas de descrever um fenótipo
  - Contagem
  - Categorização (e.g., branco, preto)
  - Medidas lineares (e.g., tamanho corporal, altura)
- Mas e fenótipos multivariados?
  - *Formato* do corpo, formato da pata etc
  - Processos de seleção não necessariamente podem modificar o tamanho e sim a forma
  - Evolução correlacionada: um atributo pode ser modificado não por seleção sobre ele, mas sim por ação de seleção num atributo correlacionado



## Quantifying and Comparing Phylogenetic Evolutionary Rates for Shape and Other High-Dimensional Phenotypic Data

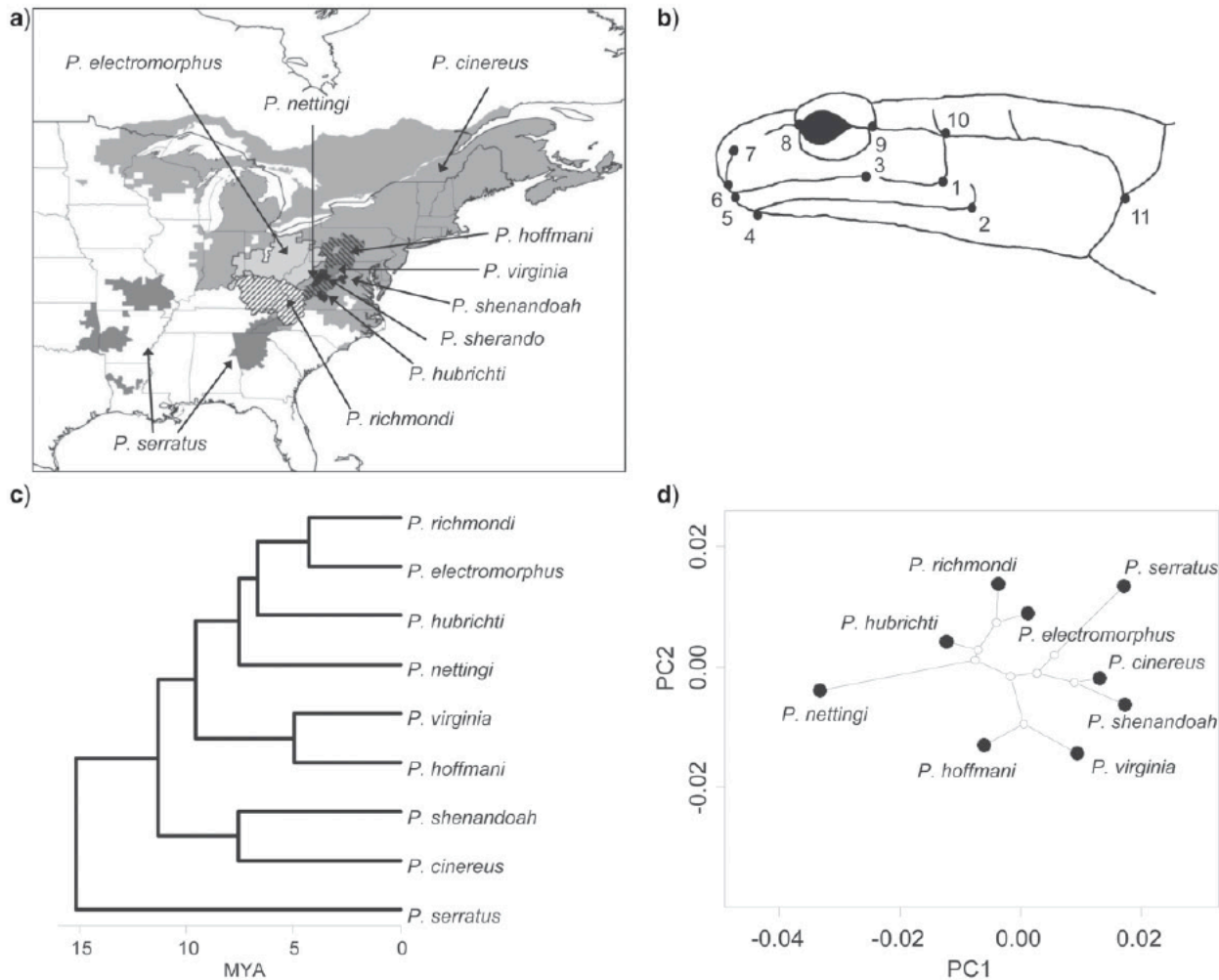
DEAN C. ADAMS<sup>1,2</sup>

<sup>1</sup>*Department of Ecology, Evolution, and Organismal Biology; and* <sup>2</sup>*Department of Statistics, Iowa State University, Ames, IA 50011, USA*

$$\sigma_{\text{mult}}^2 = \frac{\text{PD}_{U,0}^t \text{PD}_{U,0}}{N}.$$

## A Generalized $K$ Statistic for Estimating Phylogenetic Signal from Shape and Other High-Dimensional Multivariate Data

DEAN C. ADAMS\*



Salamandras do gênero *Plethodon* do leste dos EUA. Várias espécies do grupo *P. cinereus* tem distribuição restrita. Trabalhos com outros grupos demonstraram que espécies com distribuição restrita podem exibir elevadas taxas de evolução morfológica

# PGLS para traits multivariados

doi:10.1111/evo.12463



## **A METHOD FOR ASSESSING PHYLOGENETIC LEAST SQUARES MODELS FOR SHAPE AND OTHER HIGH-DIMENSIONAL MULTIVARIATE DATA**

Dean C. Adams<sup>1,2,3</sup>

# Seleção de modelos para traits multivariados

*Syst. Biol.* 67(1):14–31, 2018

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DOI:10.1093/sysbio/syx055

Advance Access publication July 13, 2017

## Multivariate Phylogenetic Comparative Methods: Evaluations, Comparisons, and Recommendations

DEAN C. ADAMS<sup>1,2,\*</sup> AND MICHAEL L. COLLYER<sup>3</sup>

*Syst. Biol.* 0(0):1–25, 2018

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DOI:10.1093/sysbio/syy045

## A Penalized Likelihood Framework for High-Dimensional Phylogenetic Comparative Methods and an Application to New-World Monkeys Brain Evolution

JULIEN CLAVEL, LEANDRO ARISTIDE, AND HÉLÈNE MORLON

**Methods in Ecology and Evolution**



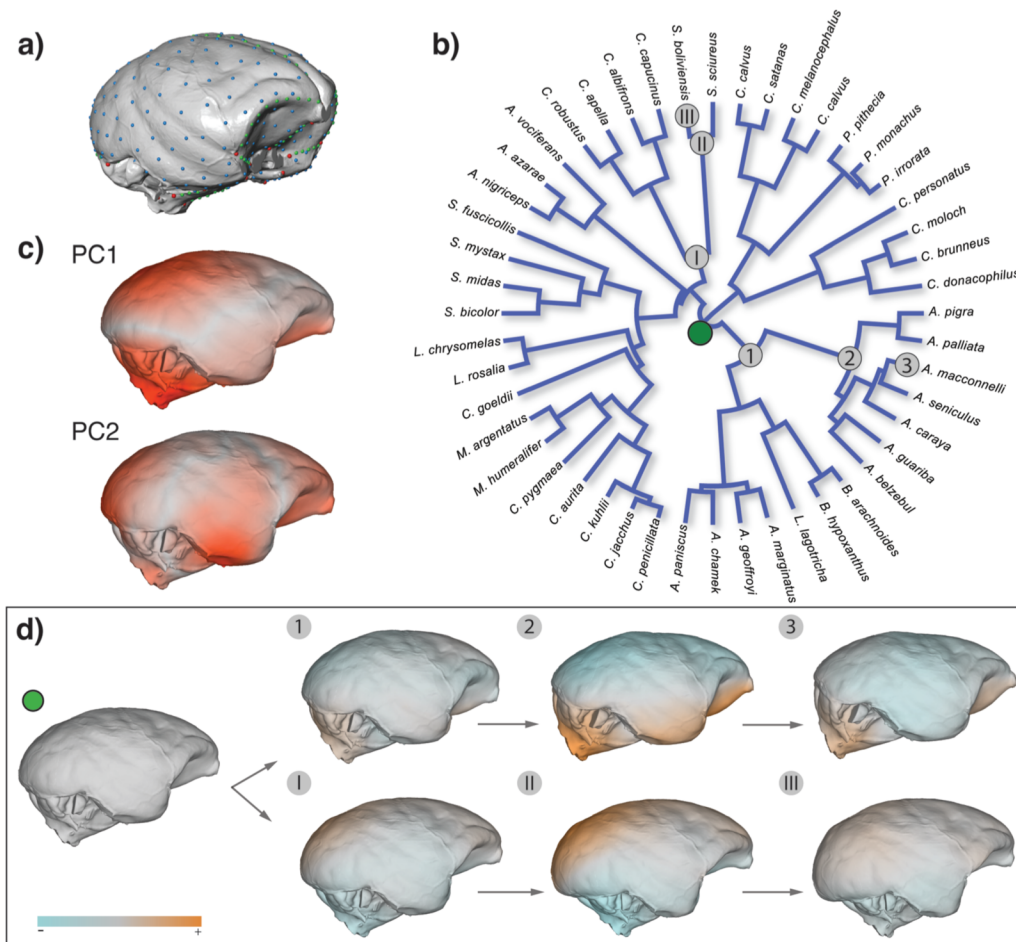
*Methods in Ecology and Evolution* 2015, 6, 1311–1319

doi: 10.1111/2041-210X.12420

APPLICATION

**mvmorph: an R package for fitting multivariate evolutionary models to morphometric data**

Julien Clavel<sup>1,2,\*</sup>, Gilles Escarguel<sup>2</sup> and Gildas Merceron<sup>3</sup>



From: A Penalized Likelihood Framework for High-Dimensional Phylogenetic Comparative Methods and an Application to New-World Monkeys Brain Evolution  
 Syst Biol. Published online June 19, 2018. doi:10.1093/sysbio/syy045  
 Syst Biol | © The Author(s) 2018. Published by Oxford University Press, on behalf of the Society of Systematic Biologists. All rights reserved. For permissions, please email: journals.permissions@oup.com This article is published and distributed under the terms of the Oxford University Press, Standard Journals Publication Model ([https://academic.oup.com/journals/pages/about\\_us/legal/notices](https://academic.oup.com/journals/pages/about_us/legal/notices))

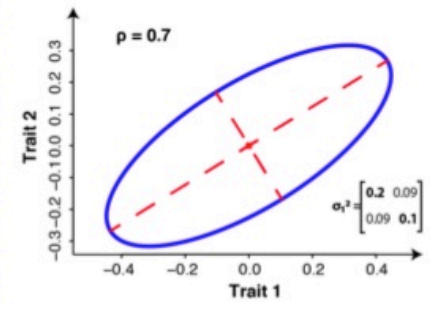
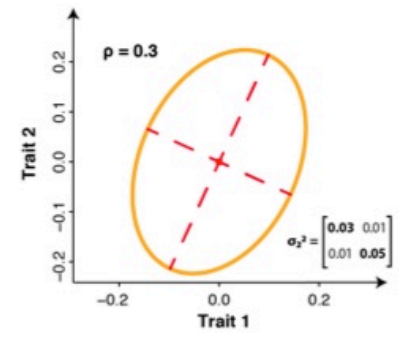
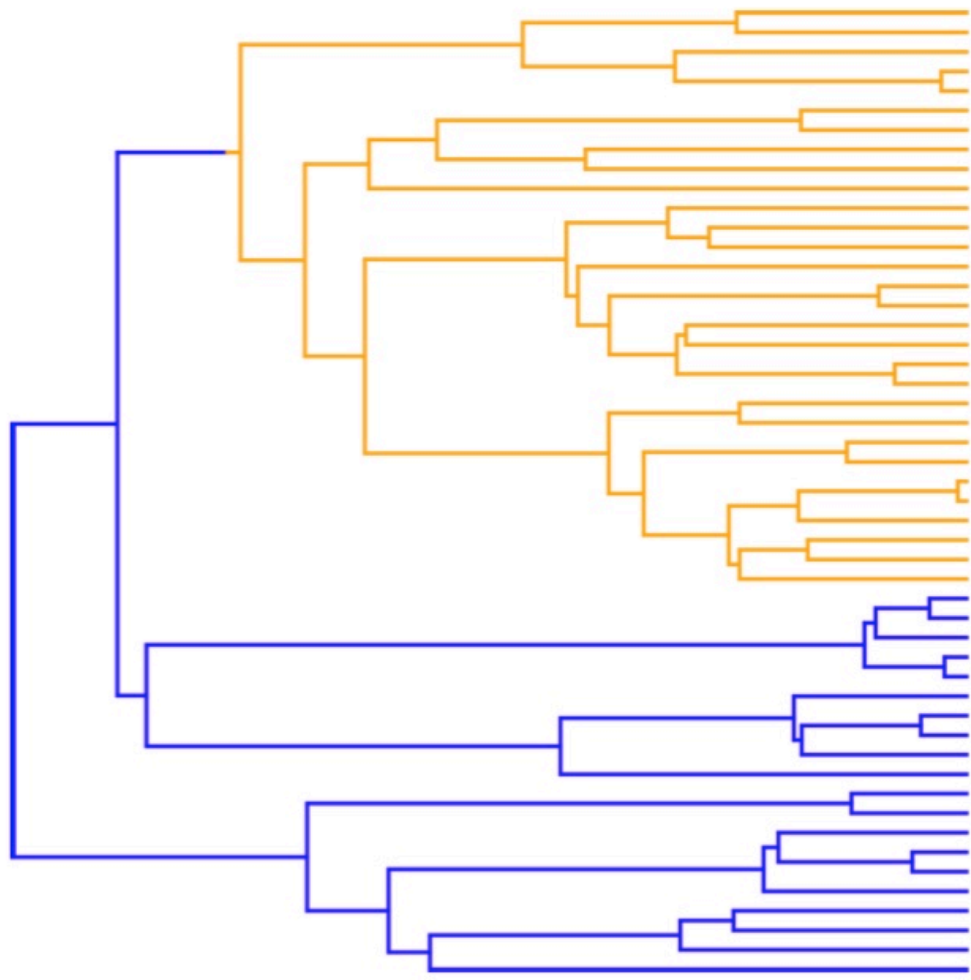
**TABLE 2.**

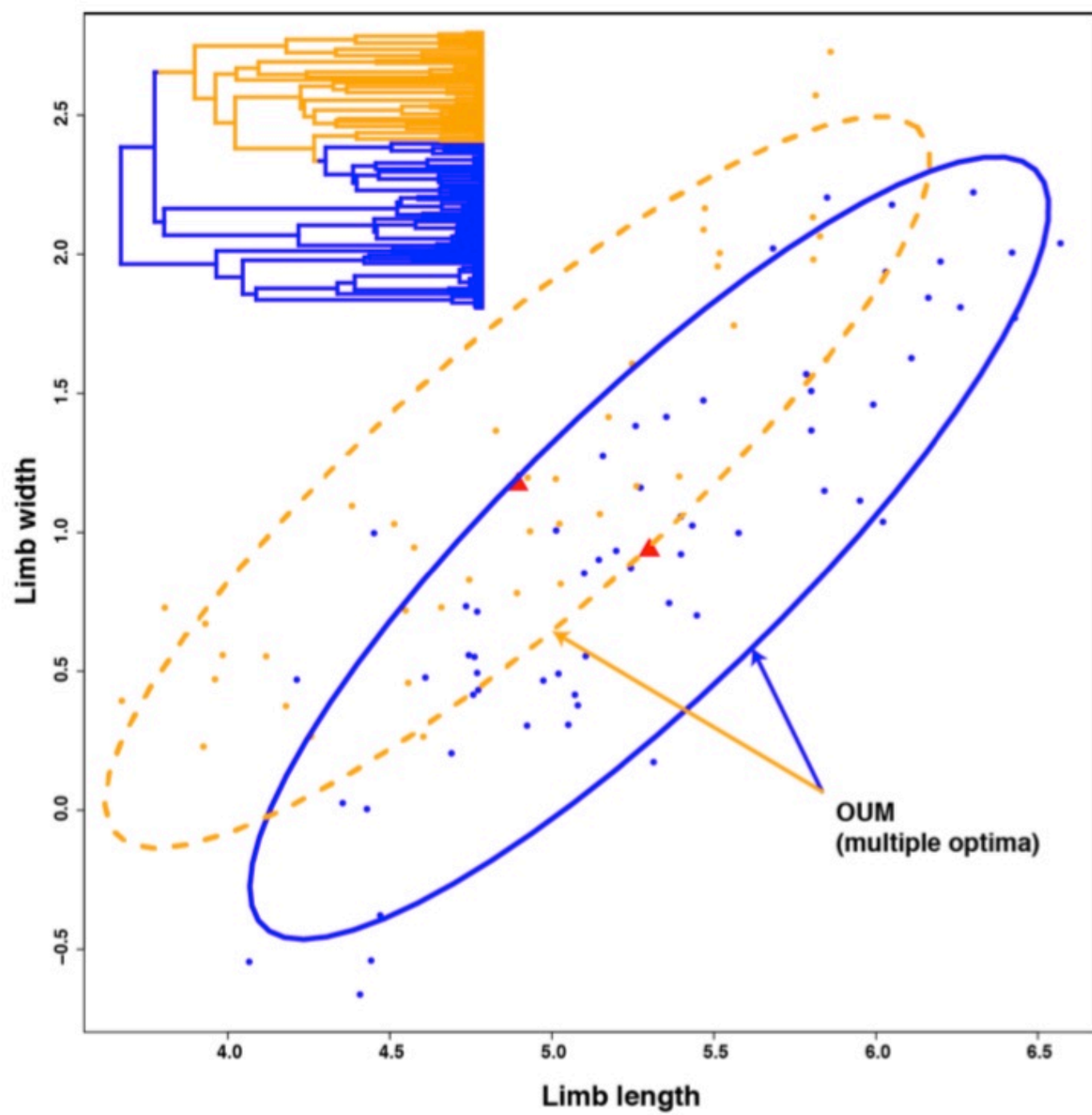
Support for BM, OU, and EB models for the evolution of New World monkeys' brain shape over 100 trees from the Bayesian posterior distribution

Model	GIC (mean $\pm$ 2 SD)	$\Delta$ GIC (2.5–97.5% range)	% trees preferred	Parameters <sup>a</sup> (mean $\pm$ 2 Sd)
BM	-726 505 $\pm$ 410	4.95–258	0	-
OU	-726 504 $\pm$ 409	1.03–260.4	3	$\alpha = 9.34 e^{-5} \pm 4.8 e^{-4}$
EB	-726 618 $\pm$ 379	0–0.30	97	$r = -0.91 \pm 0.69$

The EB model is preferred (lowest GIC value) in 97% of the trees.

<sup>a</sup>The Brownian parameters are given in the multidimensional **R** matrix (see also Fig. 4).





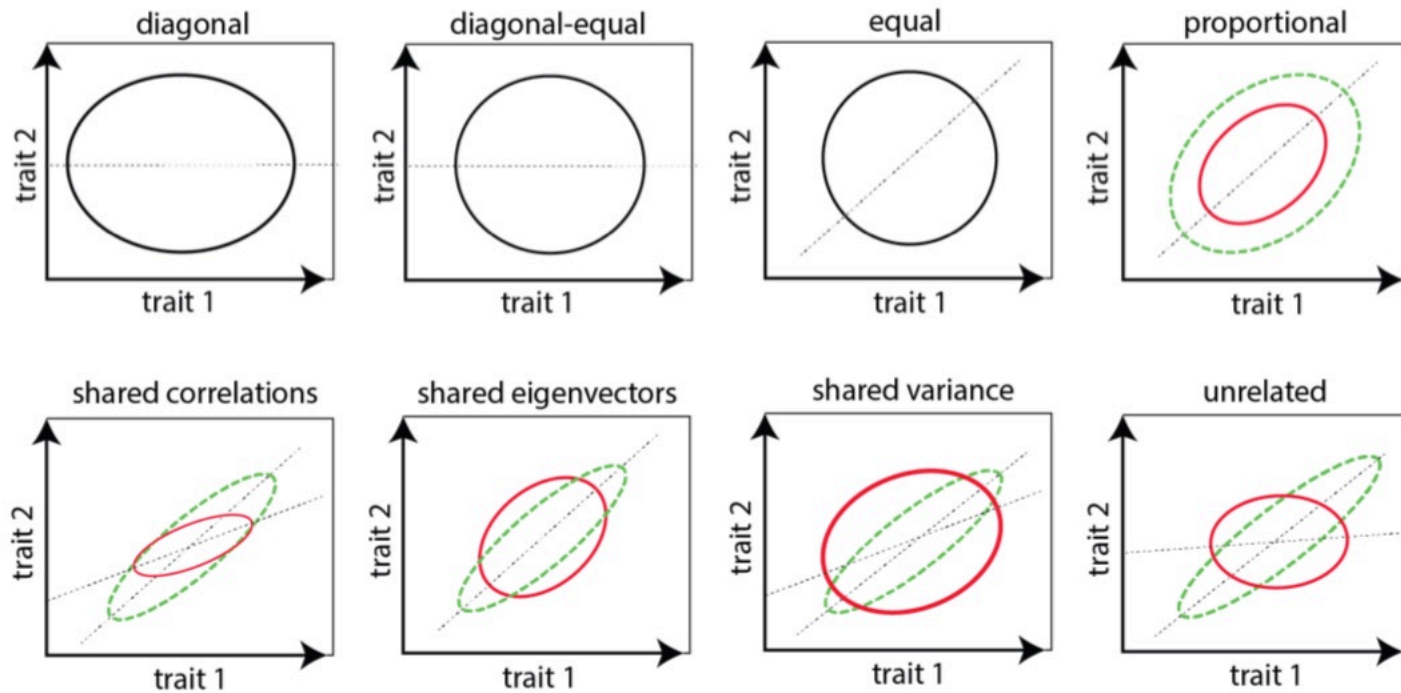


Fig. 2. Bivariate representation of the covariance constraints used in mvMORPH.

```
# Fitting the models
```

```
# BM1 - (Equal rate matrix)
```

```
model_1<-mvBM(tree, data, model="BM1", diagnostic=FALSE, echo=FALSE)
```

```
# BMM - (Proportional rate matrices)
```

```
model_2<-mvBM(tree, data, param=list(constraint="proportional")  
      , diagnostic=FALSE, echo=FALSE)
```

```
# BMM - (Shared eigenvectors between rate matrices)
```

```
model_3<-mvBM(tree, data, param=list(constraint="shared")  
      , diagnostic=FALSE, echo=FALSE)
```

```
# BMM - (Similar correlations between rate matrices)
```

```
model_4<-mvBM(tree, data, param=list(constraint="correlation")  
      , diagnostic=FALSE, echo=FALSE)
```

```
# BMM - (Similar variances between rate matrices)
```

```
model_5<-mvBM(tree, data, param=list(constraint="variance")  
      , diagnostic=FALSE, echo=FALSE)
```

```
# BMM - (Independent rate matrices)
```

```
model_6<-mvBM(tree, data, model="BMM", diagnostic=FALSE, echo=FALSE)
```

```
# Compare the models with AIC
```

```
AIC(model_1)
```

```
> [1] 37.4709
```

```
AIC(model_2)
```

```
> [1] 31.20892
```

```
AIC(model_3)
```

```
> [1] 24.68785
```

```
AIC(model_4)
```

```
> [1] 29.59168
```

```
AIC(model_5)
```

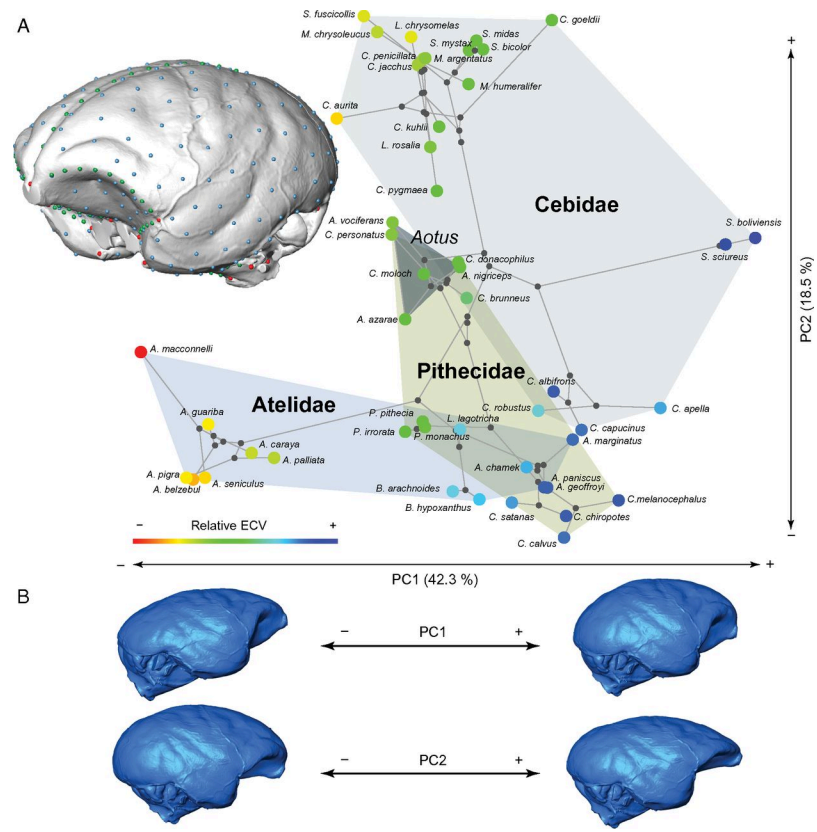
```
> [1] 38.76954
```

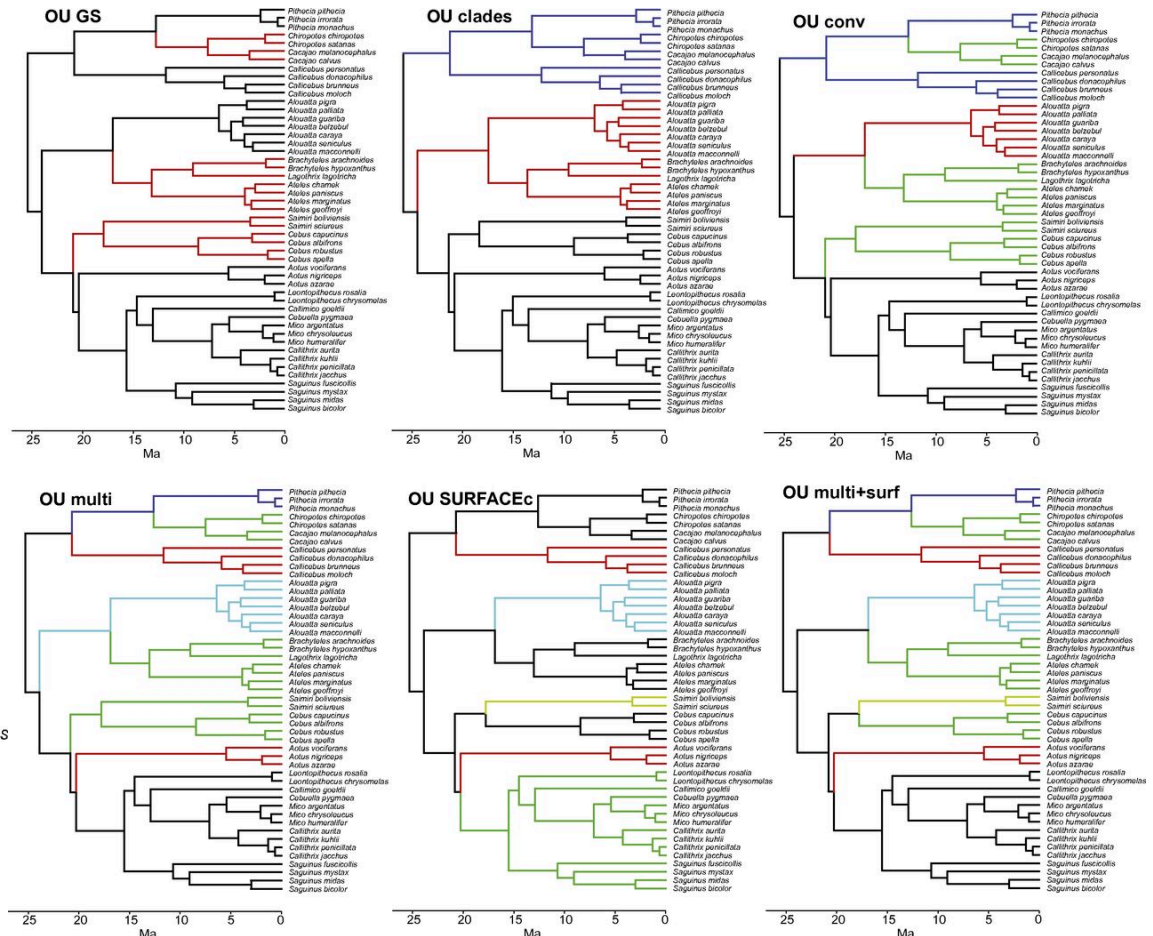
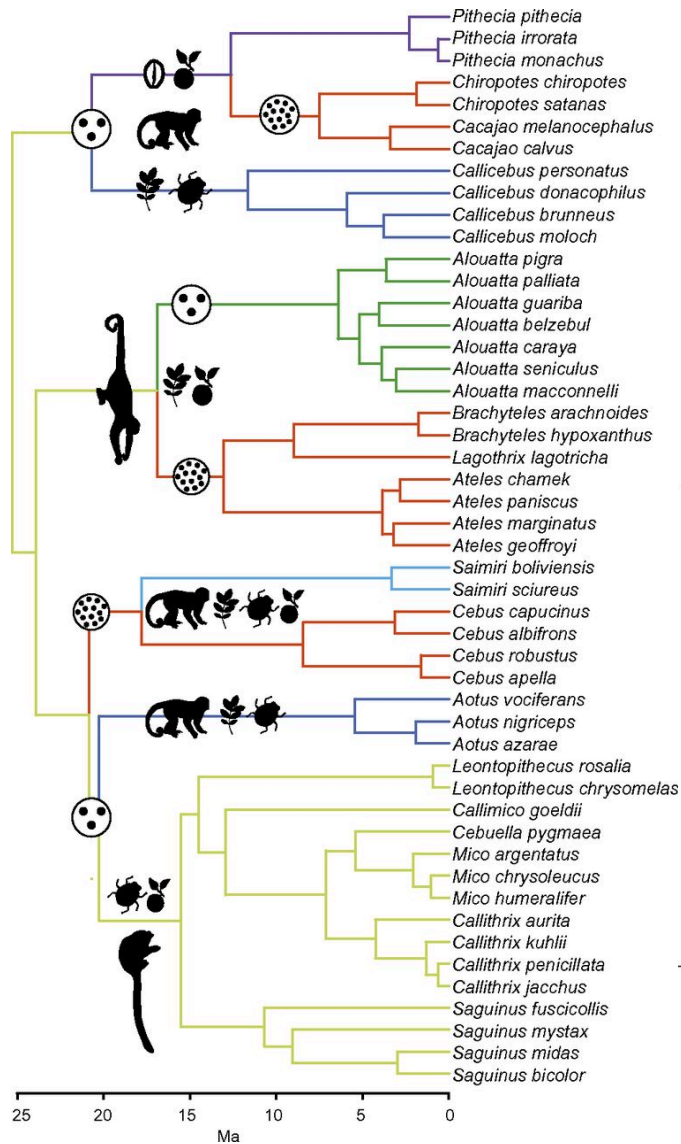
```
AIC(model_6)
```

```
> [1] 25.99354
```

# Brain shape convergence in the adaptive radiation of New World monkeys

Leandro Aristide<sup>a</sup>, Sergio Furtado dos Reis<sup>b</sup>, Alessandra C. Machado<sup>c</sup>, Inaya Lima<sup>c</sup>, Ricardo T. Lopes<sup>c</sup>, and S. Ivan Perez<sup>a,1</sup>





Modelos incluídos no mvMORPH

Resultado do SURFACE

# Mudanças de pico adaptativo levando em conta a correlação entre traits

*Syst. Biol.* 67(4):662–680, 2018

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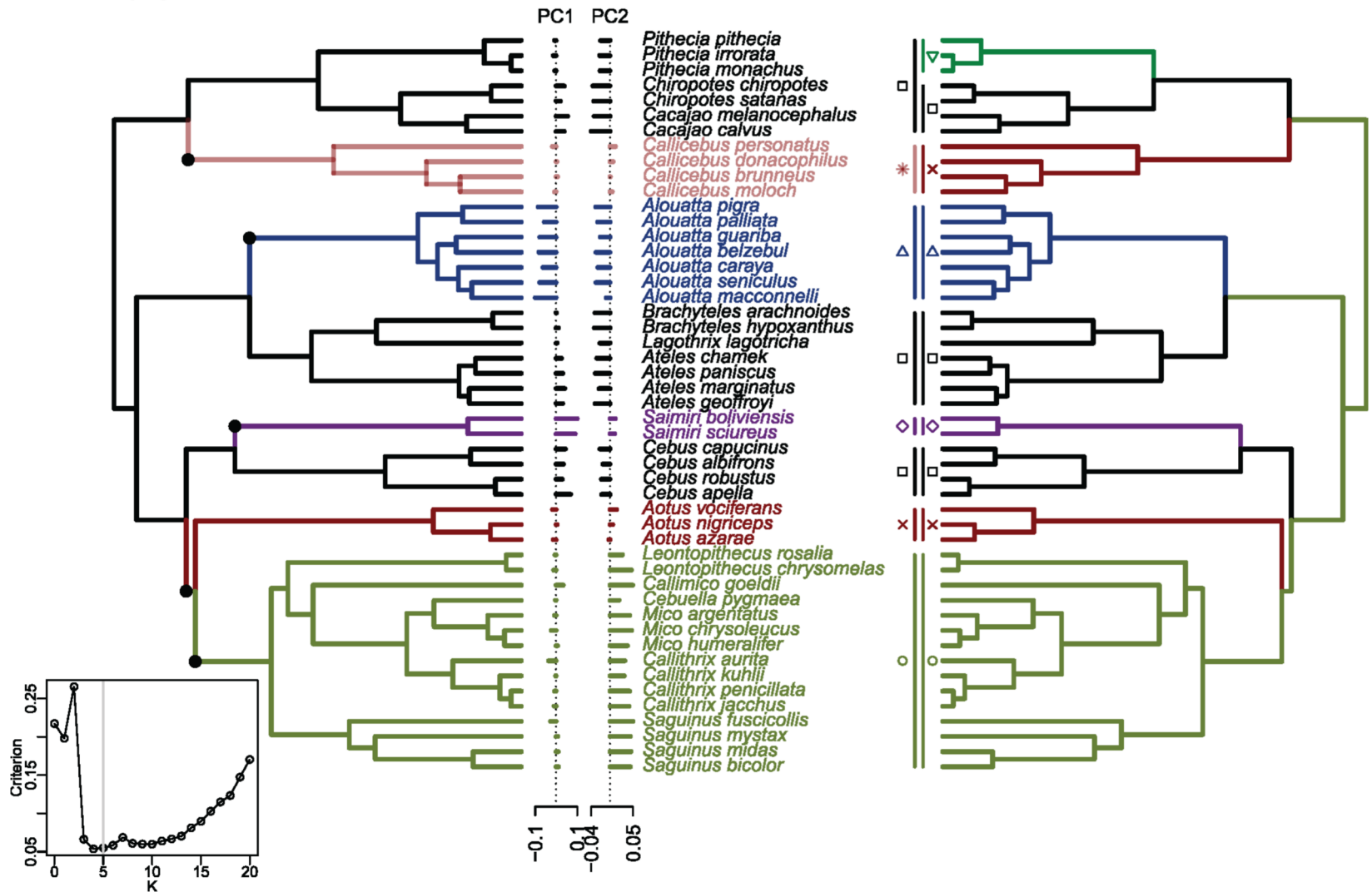
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DOI:10.1093/sysbio/syy005

Advance Access publication January 27, 2018

## **Inference of Adaptive Shifts for Multivariate Correlated Traits**

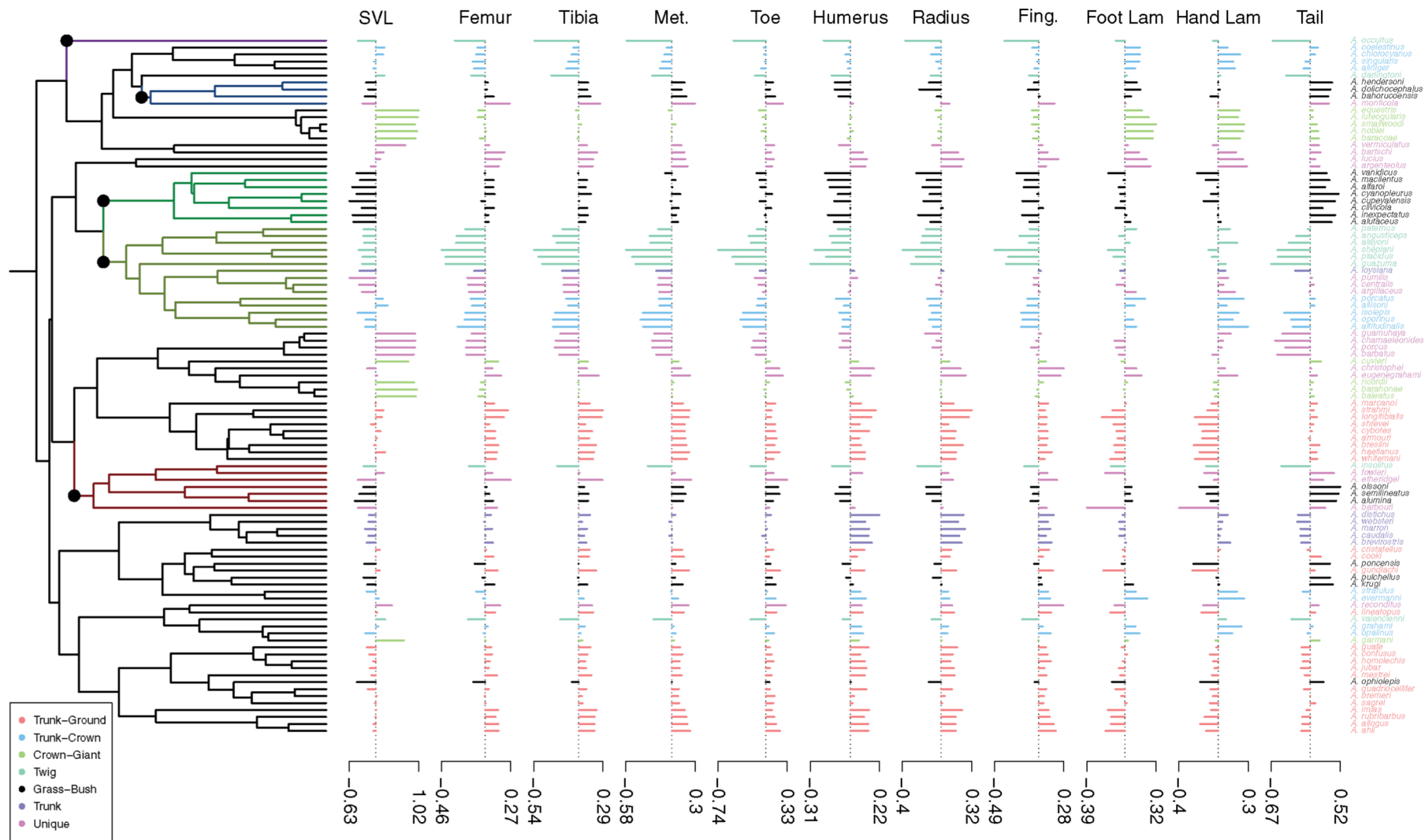
PAUL BASTIDE<sup>1,2,\*</sup>, CÉCILE ANÉ<sup>3,4</sup>, STÉPHANE ROBIN<sup>1</sup>, AND MAHENDRA MARIADASSOU<sup>2</sup>



From: Inference of Adaptive Shifts for Multivariate Correlated Traits

Syst Biol. 2018;67(4):662-680. doi:10.1093/sysbio/syy005

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From: Inference of Adaptive Shifts for Multivariate Correlated Traits

Syst Biol. 2018;67(4):662-680. doi:10.1093/sysbio/syy005

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# Modularidade e integração de fenótipos complexos

Arnold et al. *BMC Evolutionary Biology* (2017) 17:251  
DOI 10.1186/s12862-017-1101-1

BMC Evolutionary Biology

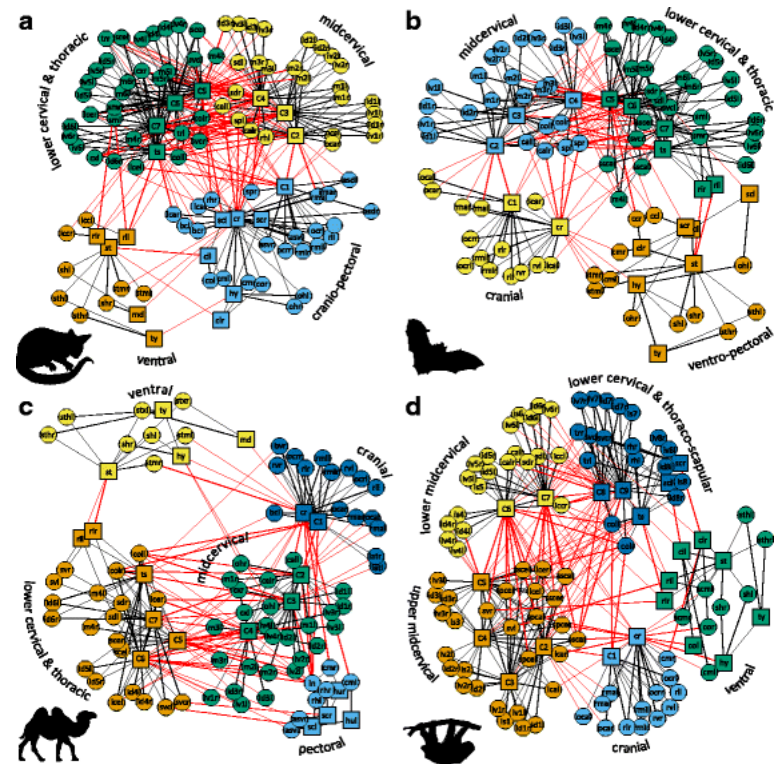
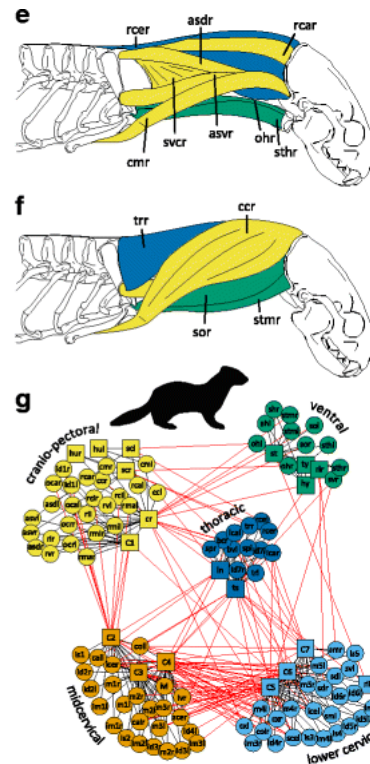
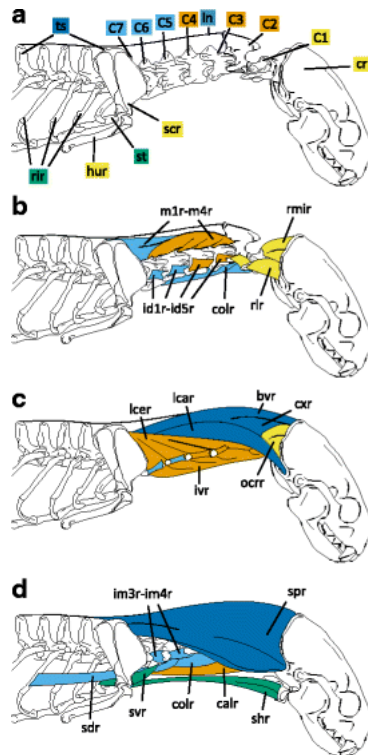
RESEARCH ARTICLE

Open Access



## Musculoskeletal networks reveal topological disparity in mammalian neck evolution

Patrick Arnold<sup>1,2\*</sup>, Borja Esteve-Altava<sup>3</sup> and Martin S. Fischer<sup>1</sup>



# Estimar taxas de evolução para diferentes módulos

Testar hipóteses de conjuntos modulares



## Methods in Ecology and Evolution



*Methods in Ecology and Evolution* 2016, 7, 565–572

doi: 10.1111/2041-210X.12511

### Evaluating modularity in morphometric data: challenges with the RV coefficient and a new test measure

Dean C. Adams<sup>1,2\*</sup>

ORIGINAL ARTICLE

doi:10.1111/evo.12743



### A new phylogenetic test for comparing multiple high-dimensional evolutionary rates suggests interplay of evolutionary rates and modularity in lanternfishes (Myctophiformes; Myctophidae)

John S. S. Denton<sup>1,2,3</sup> and Dean C. Adams<sup>4</sup>

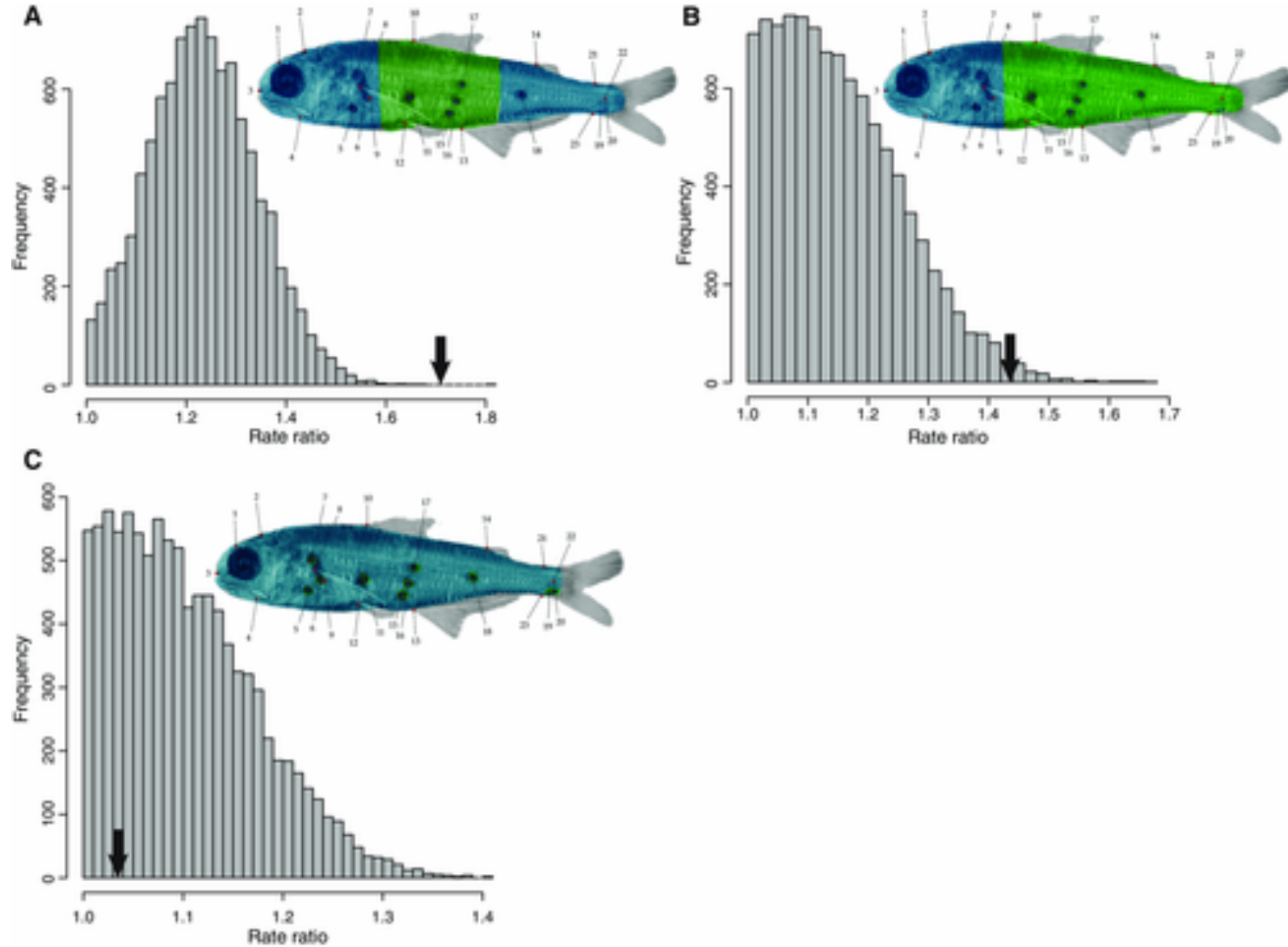
Testar taxas de evolução diferenciais para atributos envolvidos em módulos diferentes



**Table 1.** Hypotheses of modularity examined in this study, with landmark designations for each hypothesis and the predictions of each hypothesis with respect to relative rates, covariation, and modularity.

Hypothesis	Landmarks in set	Predictions		
		Rates	Covariation	Modularity
Growth gradients (H1)	M1: 1–9, 14, 18–23	$\sigma^2_{M1} > \sigma^2_{M2}$	–	H1
	M2: 10–13, 15–17			
Maneuverability/acceleration (H2)	M1: 1–9	$\sigma^2_{M1} \neq \sigma^2_{M2}$	–	H2
	M2: 10–23			
Information 1 (H3a)	M1: 1–4, 8–10, 12–14, 21–23	$\sigma^2_{M1} < \sigma^2_{M2}$	Strong	H3
	M2: 5–7, 11, 15–20			
Information 2 (H3b)		$\sigma^2_{M1} = \sigma^2_{M2}$	Weak or none	No prediction
Information 3 (H3c)		$\sigma^2_{M1} = \sigma^2_{M2}$	Strong	H1 or H2

A new phylogenetic test for comparing multiple high-dimensional evolutionary rates suggests interplay of evolutionary rates and modularity in lanternfishes (Myctophiformes; Myctophidae)



A new phylogenetic test for comparing multiple high-dimensional evolutionary rates suggests interplay of evolutionary rates and modularity in lanternfishes (Myctophiformes; Myctophidae), Volume: 69, Issue: 9, Pages: 2425-2440, First published: 17 August 2015, DOI: (10.1111/evo.12743)

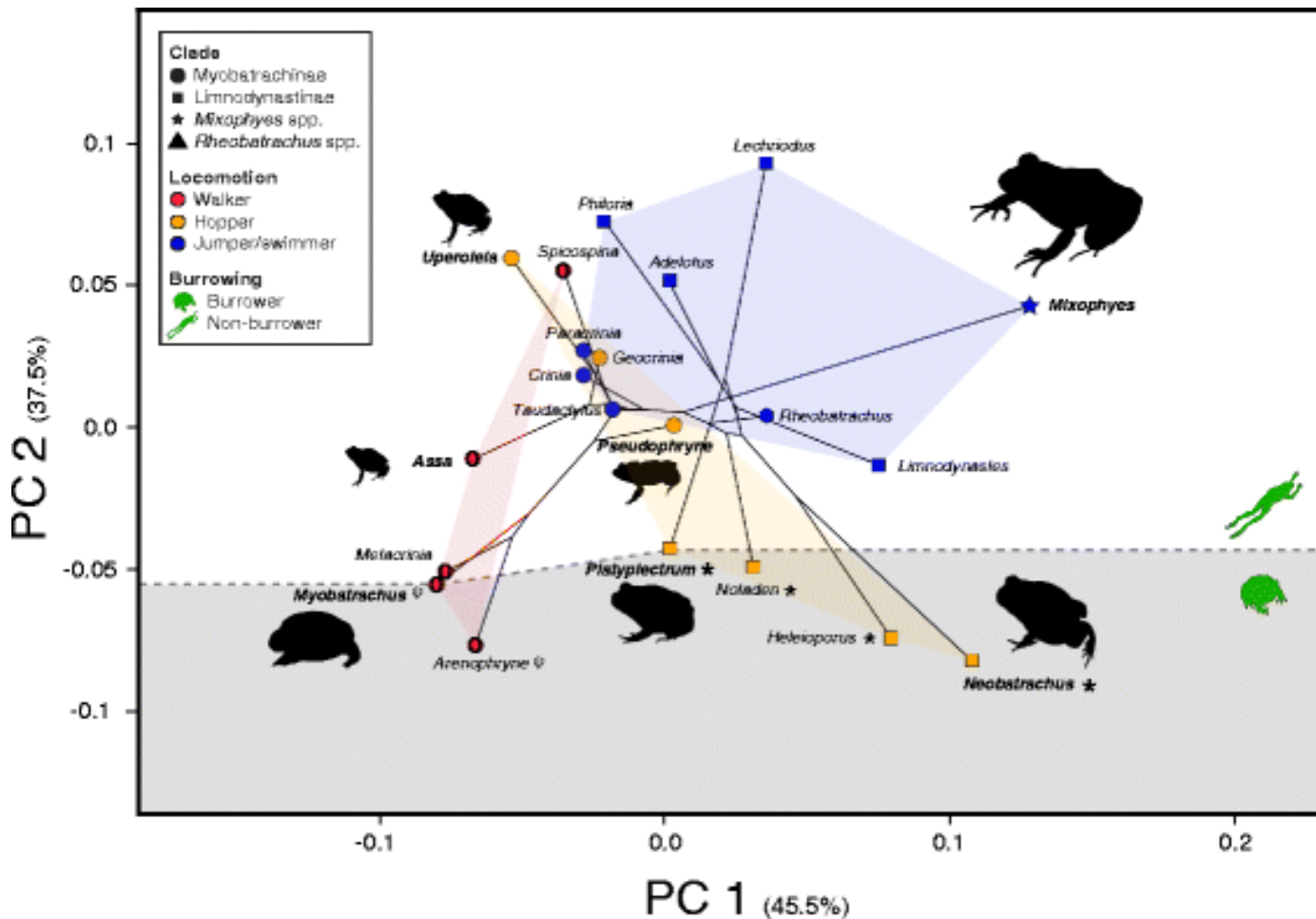
RESEARCH ARTICLE

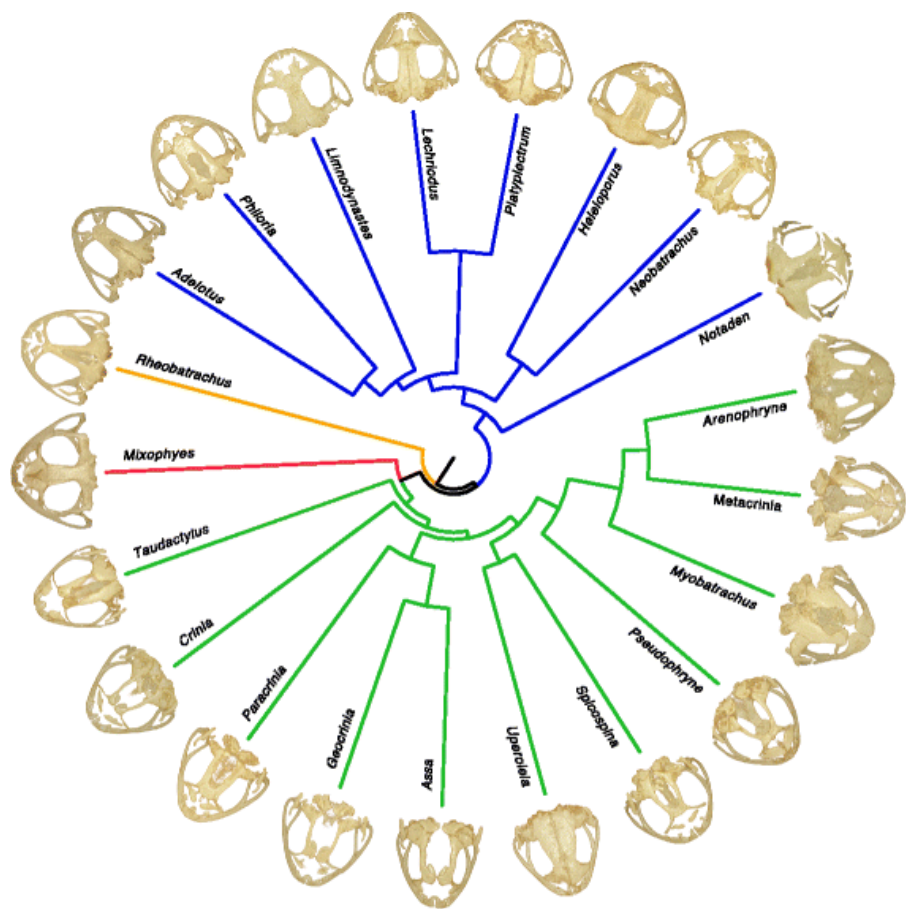
Open Access



# Phylogenetic conservatism in skulls and evolutionary lability in limbs – morphological evolution across an ancient frog radiation is shaped by diet, locomotion and burrowing

Marta Vidal-García<sup>1</sup> and J. Scott Keogh



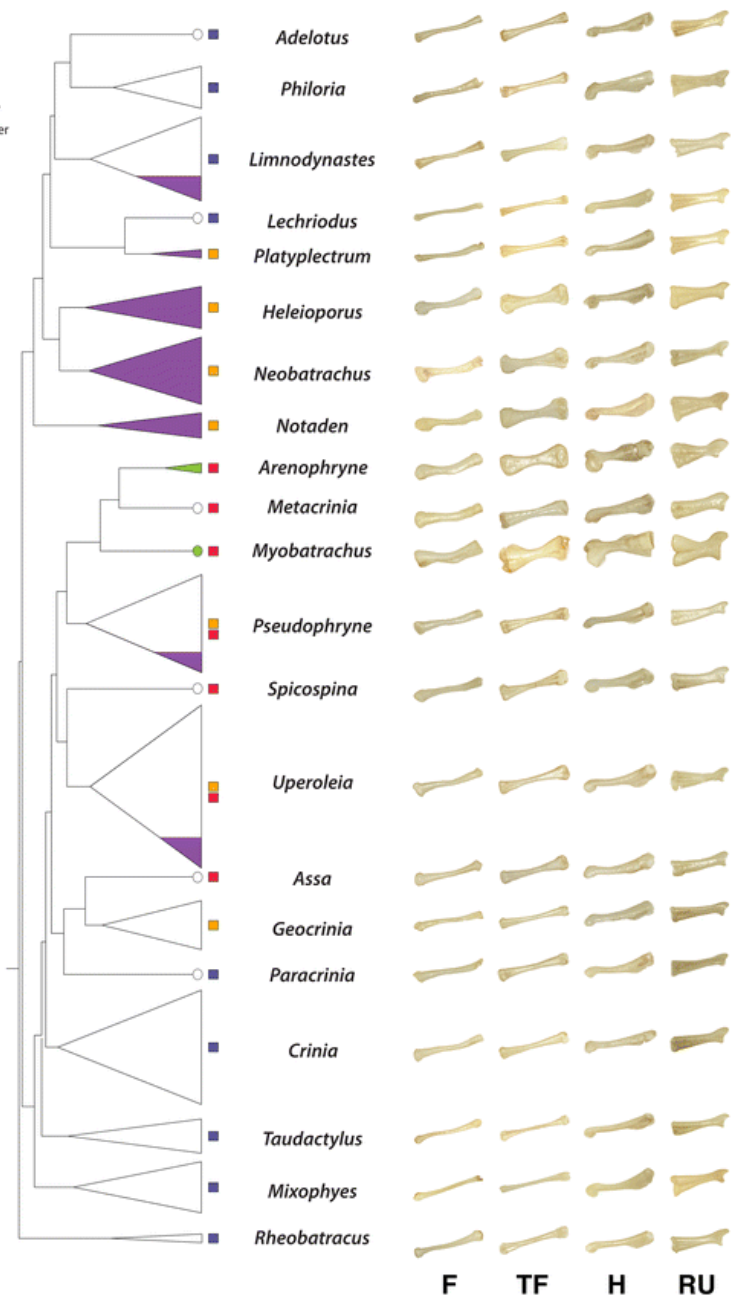


● Myobatrachinae ● Limnodynastinae ● *Mixophyes* spp. ● *Rheobatrachus* spp.



**Burrowing**  
 ● Forward burrower  
 ● Backward burrower  
 ○ Non-burrower

**Locomotor mode**  
 ■ Walker  
 ■ Hopper  
 ■ Jumper/swimmer



F TF H RU